

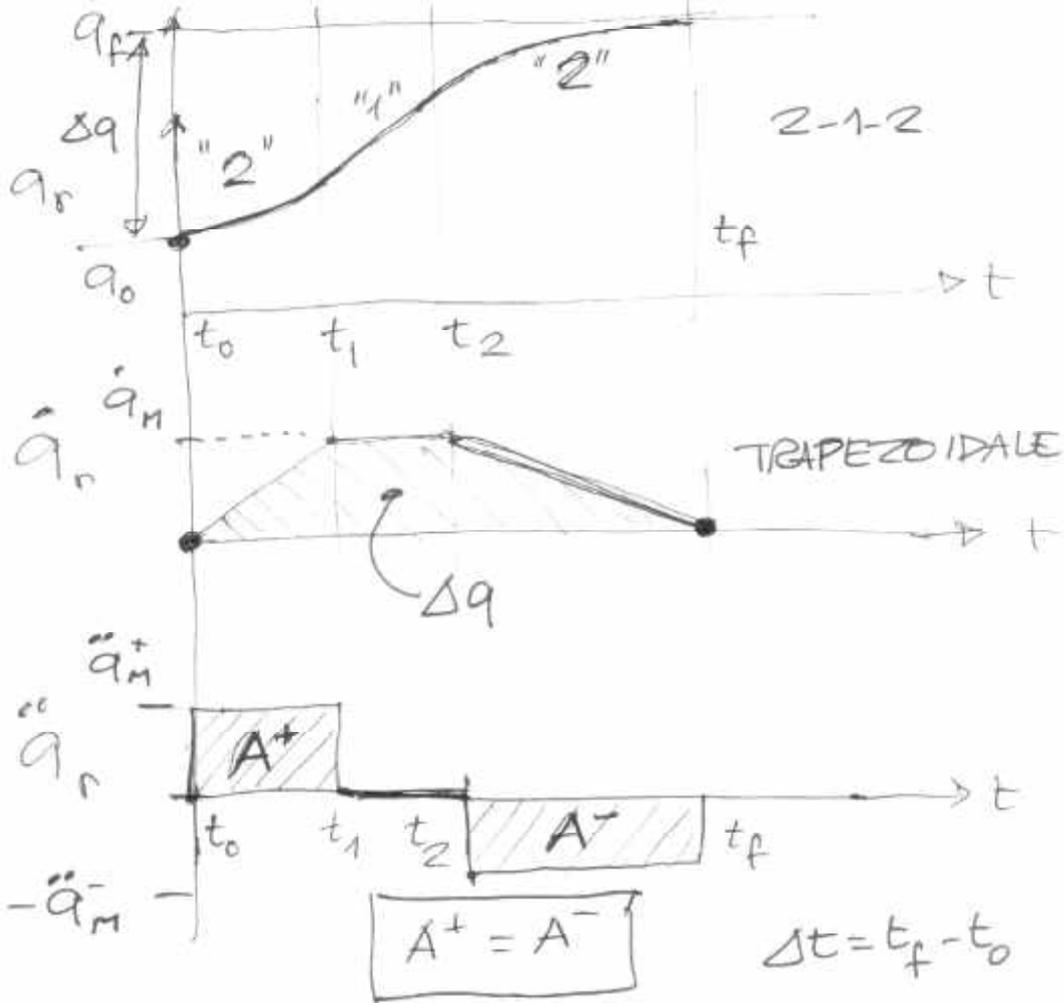
**Lezione 17/03/2004**

- a) Pianificazione della traiettoria e del riferimento: testo pagg. 127-133

17/03/04



# PIANIFICAZIONE DEL MUOTO



tempo minimo (vincolato)

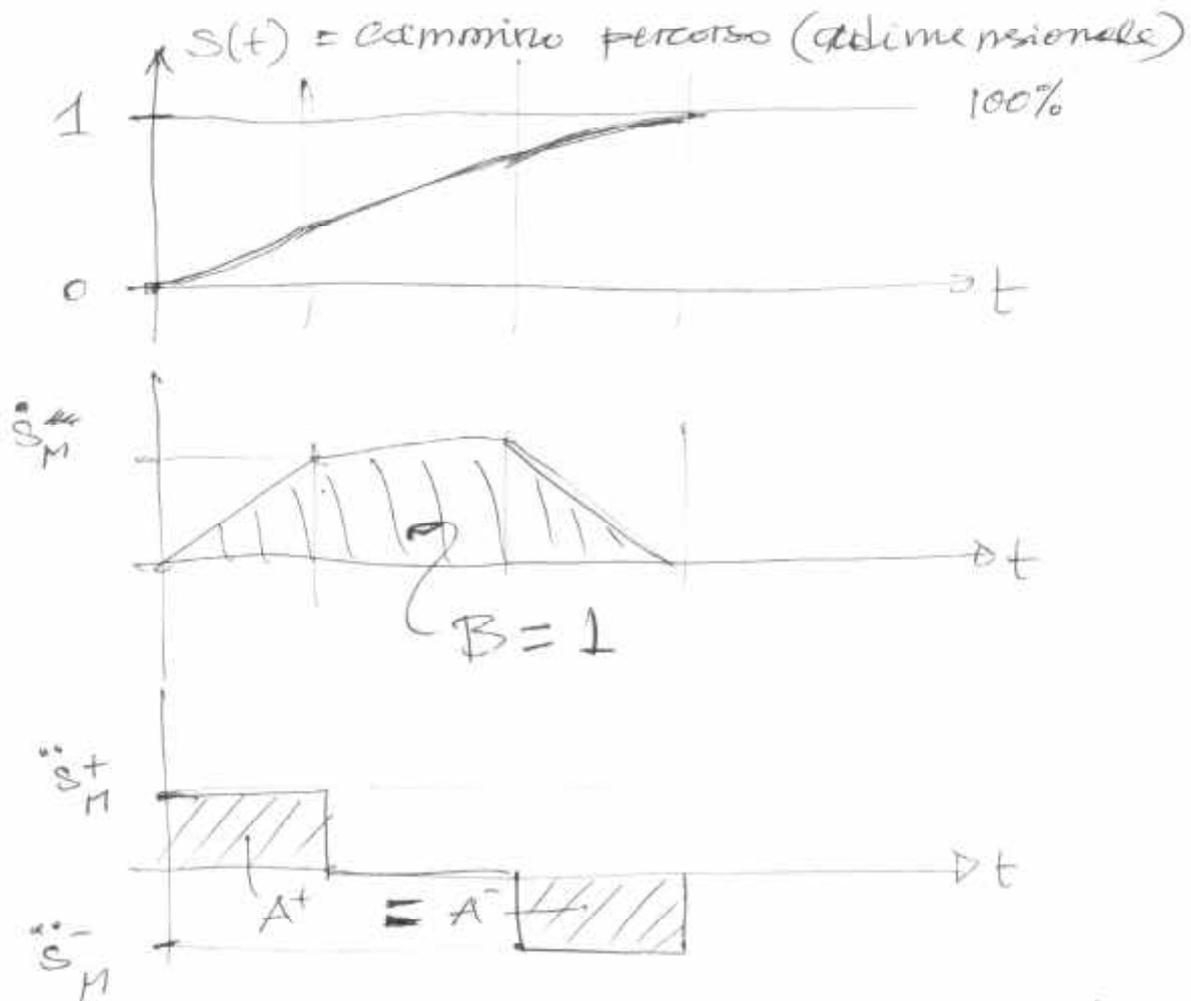
$$\overset{\text{ooo}}{\ddot{q}} \equiv \text{jerk}$$

# PIANIFICAZIONE FATTA

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(2)

CON APPROCCIO = FOTO COORDINATO



$$t_1 - t_0 = \frac{\dot{s}_M}{\ddot{s}_M^+}$$

$$t_2 - t_1 = \frac{1}{\dot{s}_M} - \frac{1}{2} \left[ \frac{\dot{s}_M}{\ddot{s}_M^+} + \frac{\dot{s}_M}{\ddot{s}_M^-} \right]$$

se  $\frac{1}{2} \left[ \frac{\dot{s}_M}{\ddot{s}_M^+} + \frac{\dot{s}_M}{\ddot{s}_M^-} \right] \gg \frac{1}{\dot{s}_M}$   
 allora traiettoria  
 triangolare



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3

$s(t)$  calcolato da una  
routine

$$\dot{s}(t)$$

$$\ddot{s}(t)$$

$$\underline{q}(t) = \underline{q}_0 + s(t)(\underline{q}_f - \underline{q}_0) = \underline{q}_0 + s(t)\underline{\Delta q}$$

combinazione convessa  
lineare

$$= \underline{q}_0 + s(t)\underline{q}_f - s(t)\underline{q}_0 =$$

$$= (1-s(t))\underline{q}_0 + s(t)\underline{q}_f$$

$$= \alpha \underline{q}_0 + \beta \underline{q}_f$$

$$\alpha + \beta \leq 1$$

$$\dot{\underline{q}}(t) = \dot{s}(t)\underline{\Delta q}$$

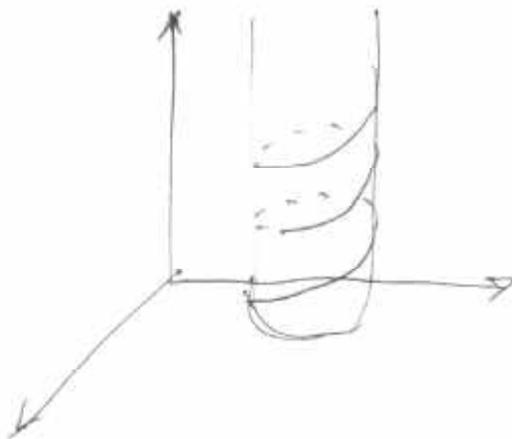
$$\ddot{\underline{q}}(t) = \ddot{s}(t)\underline{\Delta q}$$

PIANIFICAZIONE  
VARIABILI CARTESIANE

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$$\begin{aligned} \underline{p} &= f(\underline{q}) && \text{CIN DIRETTA POS} \\ \underline{q} &= f^{-1}(\underline{p}) && \text{" INVERSA POS} \\ \underline{\dot{p}} &= J(\underline{q})\underline{\dot{q}} && \text{" DIRETTA VEL} \\ \underline{\dot{q}} &= J^{-1}(\underline{q})\underline{\dot{p}} && \text{" INVERSA VEL} \end{aligned}$$



CERCHIO

$$\begin{aligned} x(t) &= R \sin(\theta(t)) + Z(t) \\ y(t) &= R \cos(\theta(t)) + Z(t) \\ z(t) &= h(t) \end{aligned}$$

CURVA CENERNA



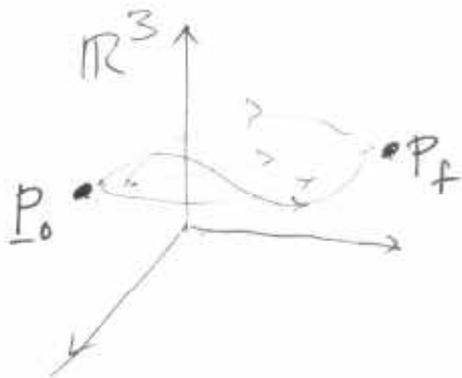
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5

CURVA MONODIMENSIONALE IN  $\mathbb{R}^3$

$$\delta(\underbrace{q(\alpha(t))}_\uparrow) = 0$$

PIANIF.  
PUNTO PUNTO



PIANIF.  
CONTINUA

