

CINEMATICA

$$\underbrace{\underline{p}; \dot{\underline{p}}}_{\text{CARTESIANO}} \leftrightarrow \underbrace{\underline{q}; \dot{\underline{q}}}_{\text{GIUNTI}}$$

STATICA

$$\underline{f}, \underline{N} \leftrightarrow \underline{\tau}$$

DINAMICA

NON LA
TRATTIANO

$$\underline{\ddot{q}} \quad \underline{\dot{q}} \quad \underline{q}$$

$$H(\underline{q})\ddot{\underline{q}}(t) + C(\dot{\underline{q}}, \underline{q})\dot{\underline{q}}(t) + \underline{g}(\underline{q}) = \underline{\tau}(t)$$

forze generalizz.
di comando

se il robot interagisce con
ambiente

$$\dots = \underline{\tau}(t) + \underline{J}^T \underline{F}$$

forze di
scambio

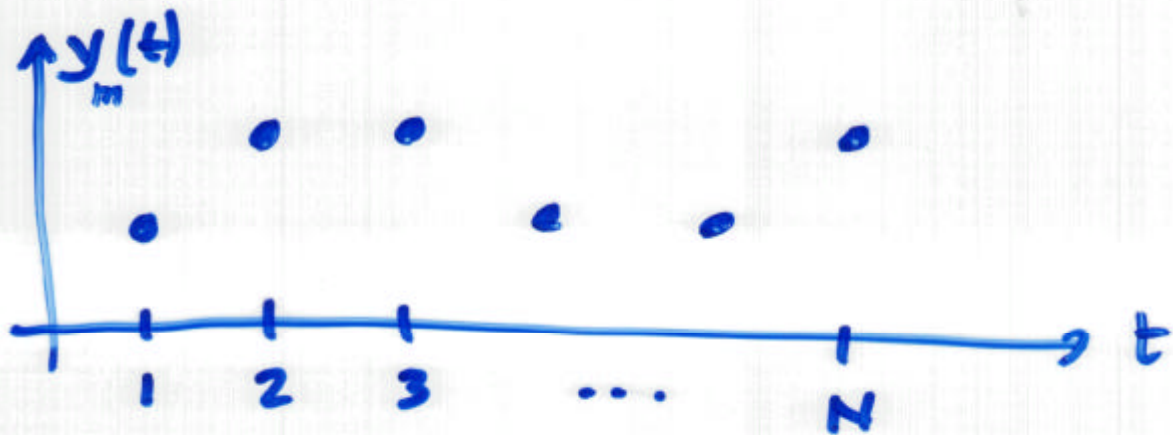
IDENTIFICARE IL MODELLO
STIMARE I PARAMETRI



- CREARE UNA FUNZIONE DELL'ERRORE TRA DATI REALI E DATI SIMULATI, FUNZIONE DEI PARAMETRI INCOGNITI
- MINIMIZZO LA FUNZ. RISPETTO AI PARAMETRI.

ESEMPIO

ABBIAMO 10 DATI SPERIMENTALI



MODELLO DI COSTANTE

$$y(t) = c$$

FUNZIONE ERRORE

$$\sum_{i=1}^N (y_m(t_i) - y(t_i))^2 \geq 0$$



$$\sum_{i=1}^N (y_m(t_i) - c)^2$$

$$c^* = \min_c \sum_{i=1}^N (y_m(t_i) - c)^2$$

LSM
LEAST SQUARE
METHOD



$$[c \quad \alpha' \quad \alpha^3 \dots \alpha^{n-1}] \begin{bmatrix} f_1^r \\ \vdots \\ f_{n-1}^r \\ 1 \end{bmatrix}$$

$$N2 \quad \lambda_n(f) = c + \alpha' f^1 + \dots + \alpha^{n-1} f_{n-1}^r$$

$$N3 \quad \lambda_n(f) = c + \alpha' f^1 + \alpha^3 f_3^r \quad c' \alpha' \alpha^3$$

$$N5 \quad \lambda_n(f) = c + \alpha f^1 \quad c' \alpha$$

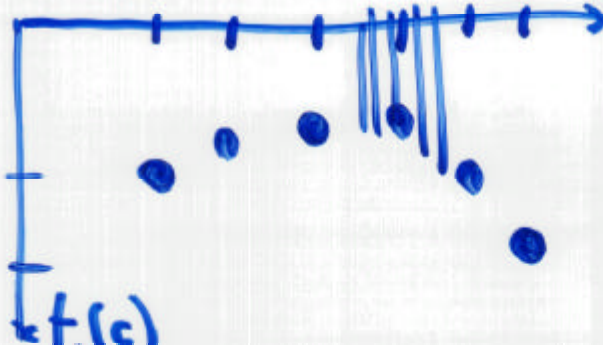
$$N7 \quad \lambda_1(f) = c \quad c$$

MODULO PIKEVISE NEI ΒΥΣΤΗΜΕΣ



2 0 3 8 0 10 c

$$c_* = 8$$



$$\begin{bmatrix} 1 & t_i & t_i^2 & \dots & t_i^{n-1} \end{bmatrix} \begin{bmatrix} \hat{a}_1 \\ \vdots \\ \hat{a}_{n-1} \end{bmatrix}$$

$\Phi_i^T \underline{\lambda}$

$$i = 1, \dots, N$$

$$\begin{bmatrix} \Phi_1^T \\ \vdots \\ \Phi_N^T \end{bmatrix} \begin{bmatrix} \lambda \end{bmatrix} = \Phi \underline{\lambda}$$

PARAMETRI INCOGNITI

MATRICE DEL
REGRESSORE

$N \times n = n \times 1$

$$\boxed{N \times 1}$$

$$\Phi \underline{\lambda} \simeq \underline{y}_m(t_i) = \begin{bmatrix} y(t_1) \\ \vdots \\ y(t_N) \end{bmatrix}$$

MODELLO $\uparrow$ DATI

$N \times 1$

$$\underline{\lambda}^* = (\Phi^T \Phi)^{-1} \Phi^T \underline{y}_m$$

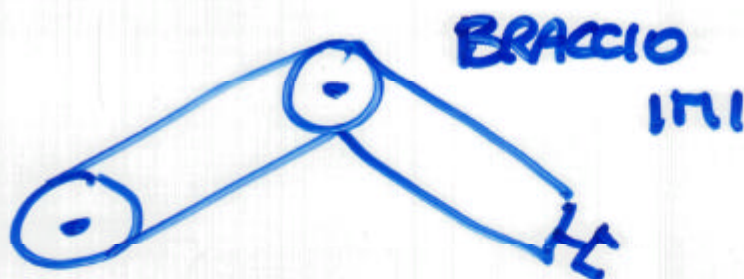
MATRICE DI PROIEZIONE

LEAST SQUARE

$$H\ddot{q} + C\dot{q} + g = \Phi \underline{\theta}$$

REGRESSORE PARAMETRI

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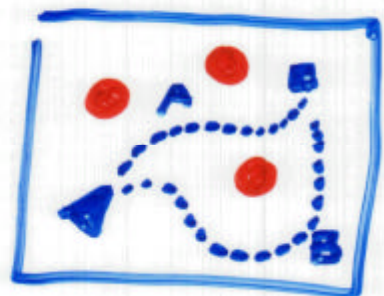


CONTROLLO

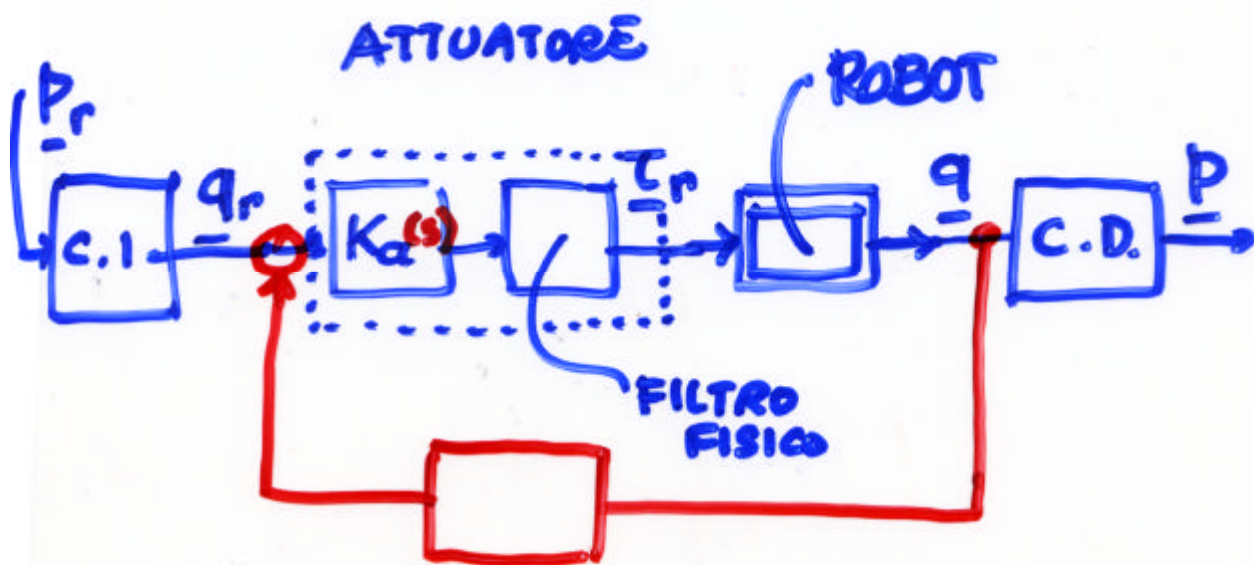
PIANIFICAZIONE

TOP-DOWN

- OBIETTIVO
- COMPITO / TASK
- OPERAZIONE
- MOSSA / MOVE
- TRAIETTORIA / CAMMINO
- RIFERIMENTO



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