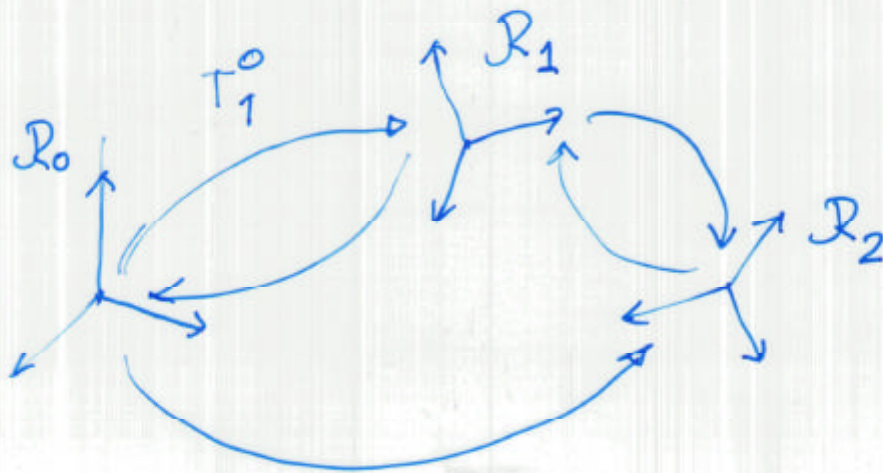




R_1^0

- trasforma $\underline{U}_{AB}^1$ in $\underline{U}_{AB}^0$
- rappresenta $\mathcal{R}_1$ in $\mathcal{R}_0$
- rappresenta il moto (di rotaz) che "prende" $\mathcal{R}_0$ e lo "porta su" $\mathcal{R}_1$

— O —

- COSA FACCIO $\begin{cases} \text{ROTAZIONE} \\ \text{e/o} \\ \text{TRASLAZIONE} \end{cases}$
 - RISPETTO A QUALE RIFERIMENTO LO FACCIO
SE RISPETTO A RIFERIMENTO "FISSO"
" " " " "MOBILE"
- | | |
|-----------------|--------|
| POST-MULTIPICAZ | MOBILE |
| PRE - ... | FISSO |

$$v^o = R_1^o v' + t_1^o$$

$$\tilde{v}^o = T_1^o \tilde{v}_1$$

$T_1^o = ?$ 4×4
matrice di trasformazione
omogenea
e rappresenta una
auto-traslazione

$$T_1^o = \left[\begin{array}{c|c} R_1^o & t_1^o \\ \hline \underbrace{0 \ 0 \ 0}_{0^T} & 1 \end{array} \right]$$

$3 \times 3 \quad 3 \times 1$

$$\tilde{v}^o = T_1^o \tilde{v}_1 = \left[\begin{array}{c|c} \boxed{R_1^o} & t_1^o \\ \hline 0^T & 1 \end{array} \right] \left[\begin{array}{c} v'_x \\ v'_y \\ v'_z \\ 1 \end{array} \right] = \underbrace{R_1^o \begin{bmatrix} v'_x \\ v'_y \\ v'_z \end{bmatrix} + t_1^o \cdot 1}_{\begin{bmatrix} R_1^o v' + t_1^o \\ \vdots \\ 1 \end{bmatrix}}$$

$$T_1^0 = \left[\begin{array}{c|c} R_1^0 & \underline{t}_1^0 \\ \hline 0^T & 1 \end{array} \right]$$

CASI ELEMENTARI

0) NULLA

$$T_1^0 = \left[\begin{array}{c|c} I & 0 \\ \hline 0^T & 1 \end{array} \right] \equiv I_{4 \times 4}$$

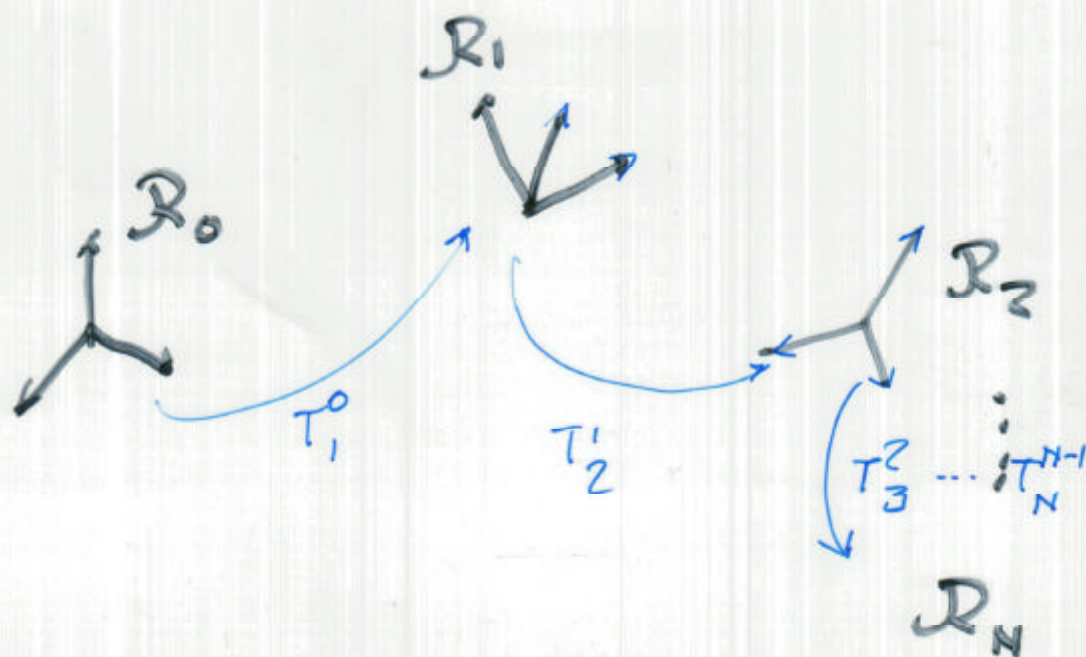
1) SOLO TRASLAZIONE = TRASL. "PURA"

$$T_1^0 = \left[\begin{array}{c|c} I & \underline{t}_1^0 \\ \hline 0^T & 1 \end{array} \right]$$

2, 3, 4) ROTAZIONI PURE

INTORNO ASSE $\begin{matrix} X \\ Y \\ Z \end{matrix}$

$$T_1^0 = \left[\begin{array}{c|c} R_1^0 & \underline{0} \\ \hline \underline{0^T} & 1 \end{array} \right] \text{ STRUTTURALE}$$



$$T_N^0 = ? = T_1^0 T_2^1 T_3^2 \dots T_{N-1}^{N-2} T_N^{N-1}$$

— o —

$$T_1^0 = \begin{bmatrix} R_1^0 & t_1^0 \\ 0^T & 1 \end{bmatrix}$$

$$(T_1^0)^{-1} \equiv T_0^1$$

$$T_1^0 T_0^1 = T_0^0 = I$$

$$T_0^1 \left[\begin{array}{c|c} R_0^1 & -R_0^1 t_1^0 \\ \hline 0^T & 1 \end{array} \right]$$

$$R_0^1 = (R_1^0)^{-1} \\ = (R_1^0)^T$$